Computer Science G12

Howework (To be discussed Wed 1 Nov 2017)

Consider the grammar given by the alphabet $\Sigma = \{x, y, z, (,), +, -, *, /\}$, the start symbol S, and the following production rules:

 $\begin{array}{ll} 1. \hspace{0.1cm} S \rightarrow x \\ 2. \hspace{0.1cm} S \rightarrow y \\ 3. \hspace{0.1cm} S \rightarrow z \\ 4. \hspace{0.1cm} S \rightarrow S + S \\ 5. \hspace{0.1cm} S \rightarrow S - S \\ 6. \hspace{0.1cm} S \rightarrow S * S \\ 7. \hspace{0.1cm} S \rightarrow S/S \\ 8. \hspace{0.1cm} S \rightarrow (S) \end{array}$

The string (x + y) * x - z * y/(x + x) is a well-formed formula (wff) in this grammar, i.e., this grammar can generate that string.

Exercise: Prove this statement, i.e, prove that that string is a wff. (or rather, complete the proof that starts as shown below)

Sol.:

- 1. S [the start symbol]
- 2. S-S [rule 5]
- 3.